A Variational Database Management System

Parisa Ataei, Fariba Khan, Eric Walkingshaw^{*} Corvallis, Oregon, USA {ataeip,khanfari,walkiner}@oregonstate.edu

Abstract

Many problems require working with data that varies in its structure and content. Current approaches, such as schema evolution or data integration tools, are highly tailored to specific kinds of variation in databases. While these approaches work well in their roles, they do not address all kinds of variation and do address the interaction of different kinds of variation in databases. In this paper, we define a framework for capturing variation as a generic and orthogonal concern in relational databases. We define variational schemas, variational databases, and variational queries for capturing variation in the structure, content, and information needs of relational databases, respectively. We define a type system that ensures variational queries are consistent with respect to a variational schema. Finally, we design and implement a variational database management system as an abstraction layer over a traditional relational database management system. Using previously developed use cases, we show the feasibility of our framework and demonstrate the performance of different approaches used in our system.

CCS Concepts: • Information systems \rightarrow Relational database model; • Software and its engineering \rightarrow Software product lines.

Keywords: variation, variational data, relational databases, choice calculus, software product lines, type systems

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1 Introduction

Managing variation in databases is a perennial problem that appears in different forms and contexts [8, 11, 14, 22, 44]. In

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databases, variation arises when several database instances, which may differ in schema, content, or constraints, conceptually represent the same database. Existing work on database variation focuses on specific kinds of variation such as schema evolution [4, 13, 32, 34, 42], data integration [19], and database versioning [12, 26]. These works provide solutions specific to the kinds of variation they address, but do not provide a general-purpose solution to managing variation in databases. This is a problem since new kinds of variation often arise and different kinds of variation can interact; existing solutions are often ill-suited to these scenarios.

Schema evolution is an example of a kind of variation in databases that is well-supported [4, 13, 32, 34, 42]. In the schema evolution scenario, a database's schema changes over time as the database is extended or refactored to support new information needs, and the goal is to automatically migrate data and queries to new versions of the database. Thus, schema evolution is a kind of *variation* over the dimension of time, and each version of the database can be viewed as a *variant* of the same database.

However, other kinds of database variation are less well supported. One example arises in the context of software product lines (SPLs) [3]. An SPL arises when the same code base is used to produce multiple different variants of a software system, customized with different sets of features or tailored for different clients. Naturally, the data requirements of each variant of an SPL may differ [41]. SPL researchers have developed various encodings that allow describing variation in the data model among variants by annotating elements of the model with features from the SPL [1, 40, 41]. These solutions can generate a database schema variant for each software variant of the SPL. However, these solutions address only variation in the data model but do not extend to the level of data or queries. The lack of variation support in queries leads to unsafe techniques such as encoding different variants of query through string munging, while the lack of variation support in data precludes testing with multiple variants of a database at once.

Worse is when multiple kinds of variation interact. Although structural variation over time is well-supported by schema evolution, and structural variation in "space" is partially supported by recent SPL research, there is no support for the inevitable evolution of an SPL's variational data model [24]. Nor do existing approaches support variation across all levels of a relational database: schema, queries, and content. In previous work, we argued that schema evolution, SPL-like variation, and other forms of database variation,

^{*}The authors are currently unaffiliated. This work was performed while employed by Oregon State University.

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Temporal	Database Schema Variants for SPL Software Variants			
Features	basic	educational	Features	
V ₁	empacct (empno, name, hiredate, title, deptno)	course (courseno, coursename)	Т	
	job (title, salary)	teach (teacherno, courseno)		
	dept (deptname, deptno, managerno)	student (studentno, courseno, grade)	11	
	empbio (empno, sex, birthdate)			
V2	empacct (empno, hiredate, title, deptno, std, instr)	ecourse (courseno, coursename)		
	job (title, salary)	course (courseno, coursename, time, class)		
	dept (deptname, deptno, managerno)	teach (teacherno, courseno)	T_2	
	empbio (empno, sex, birthdate, name)	student (studentno, courseno, grade)		
	empacct (empno, hiredate, title, deptno, std, instr, salary)	ecourse (courseno, coursename, deptno)		
V	dept (deptname, deptno, managerno, stdnum, instrnum)	course (courseno, coursename, time, class, deptno)	<i>T</i> ₃	
V_3	empbio (empno, sex, birthdate, firstname, lastname)	teach (teacherno, courseno)		
		take (studentno, courseno, grade)		

Table 1. Schema variants of the en	nployee database develop	bed for multiple software variants	by an SPL.
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such as data integration and database versioning, are all facets of a similar problem that can be addressed by *treating variation as a general and orthogonal concern* in relational databases [6–8]. An advantage of treating different kinds of variation uniformly is that it is easy to support the interaction of multiple kinds of variation, and to coordinate variation in structure with corresponding variation in queries and content. We illustrate these aspects throughout the paper using a motivating example described in Section 2.

In previous work, we have proposed the idea of *variational databases* (*VDB*), which incorporate variation as a general and orthogonal concern in relational databases [6, 7]. In this paper, we significantly expand on and realize this idea through the formalization and implementation of a *variational database management system* (VDBMS). Specifically, this paper makes the following contributions:

- We define a formal model of *variational databases*, whose structure are given by a *variational schema* and whose content are given by *variational tables* (Section 4).
- We define *variational relational algebra* for querying VDB, a *static type system* for ensuring that all variants of a query are compatible with the corresponding variants of the VDB, and identify properties of VRA (Section 5).
- We implement a prototype of VDBMS as a layer on top of a traditional relational database management system (RDBMS) (Section 6) and evaluate this implementation on previously developed [8] use cases (Section 7).

2 Motivating Example

In this section, we motivate VDBMS by illustrating the scenario described in Section 1 where two kinds of database variation interact, producing a scenario that is not well supported by any existing tools. The scenario involves the evolution over time of a database-backed SPL.

An SPL uses a set of boolean variables called *features* to indicate functionality that may be included or not in each

software variant. Consider an SPL that generates management software for companies. It has a feature edu indicating whether a company provides educational resources for its employees. Software variants in which edu is enabled (i.e., edu = true) provide this additional functionality while variants where it is disabled provide only the basic functionality.

If *edu* is the only optional feature, then at any point in time, this SPL has two variants: basic and educational. However, each variant will also evolve as the SPL evolves, leading to several different basic and educational variants over time.

Each variant of the SPL needs a database to store information about employees, and the selection of features impacts the database: While basic variants do not store any education-related records, educational variants do. We visualize the impact of both features and the evolution of the schema in Table 1, where feature variation is captured in the columns and variation over time is captured in the rows. Each basic schema variant contains only one schema in column basic, while an educational schema variant consists of two sub-schemas: one from the basic column and one from the educational column. The two sub-schemas may vary over time independently. For example, an extension to the educational sub-schema may use an older version of the basic schema. This is illustrated by the highlighted cells in Table 1, which forms a complete schema for a particular educational variant. To describe variation over time of each sub-schema, we introduce two disjoint sets of temporal features (boolean variables, like any other feature), shown in the leftmost and rightmost columns.

Now, consider the following scenario: In the initial design of the basic database, the database administrator (DBA) settles on three tables *empacct*, *job*, *dept*, and *empbio*, shown in Table 1 and associated with feature V_1 . Later, they decide to add attributes *std* and *instr* to the *empacct* table, associated with feature V_1 . Since some clients' software relies on a previous design, the two schemas have to coexist in parallel. Therefore, the presence of the *std* and *instr* attributes is *variational*, they only exist in the basic schema when $V_2 = true$ and *edu* = true. This scenario is an example of *component evolution* in SPLs, where developers update, refactor, and improve components of the SPL, including the database [24].

Now, consider the case where a client that previously requested a basic variant of the software has added courses to educate its employees in specific subjects. The SPL developer needs to enable the *edu* feature for this client, forcing the adjustment of the schema variant to include the educational sub-schema. This case describes *product evolution*, where database evolution in an SPL results from clients adding/removing features/components [24].

The situation is further complicated since the basic and educational schemas are interdependent. Consider the basic schema variant for feature V_2 . Attributes *std* and *instr* only exist in the *empacct* relation when *edu* = true, represented by a dash-underline, otherwise the *empacct* relation has only the attributes *empno*, *hiredate*, *title*, and *deptno*. Hence, the attributes *std* and *instr* in *empacct* relation are *variational*, that is, they only exist in *empacct* relation when *edu* = true.

3 Preliminaries

In this section, we introduce concepts and notations that we use throughout the paper. We discuss relational concepts and their variational counterparts. Thus, for clarity, we use an <u>underline</u> to distinguish a non-variational entity from its variational counterpart, e.g., \underline{x} is a non-variational entity while x is its variational counterpart, if it exists.

3.1 Relational Databases and Relational Algebra

A relational database \underline{D} stores information in a structured manner by forcing data to conform to a *schema* \underline{S} that is a finite set $\{\underline{s}_1, \ldots, \underline{s}_n\}$ of *relation schemas*. A relation schema is defined as $\underline{s} = r(\underline{a}_1, \ldots, \underline{a}_k)$ where each $\underline{a}_i \in \underline{A}$ is an *attribute* contained in the relation named r. We assume a total order $\leq_{\underline{A}}$ on \underline{A} , and assume for simplicity that sets of attributes are sorted according to $\leq_{\underline{A}}$.

The content of database \underline{D} is stored in the form of *tuples*. A tuple \underline{u} is a list of *values*. We do not distinguish between different types of values within a relational database.¹ The values within a tuple correspond to the attributes in its corresponding relation schema, that is, given tuple $\underline{u} = (\underline{v}_1, \dots, \underline{v}_k)$ in the relation with relation schema $r(\underline{a}_1, \dots, \underline{a}_k), \underline{v}_i$ corresponds to attribute \underline{a}_i . A *relation content*, \underline{U} , is the set of all tuples $\{\underline{u}_1, \dots, \underline{u}_m\}$ corresponding to a particular relation. The operation att(i) returns the attribute corresponding to index *i* in a tuple, implicitly looking up the attribute in the corresponding relation schema. A *table* $\underline{t} = (\underline{s}, \underline{U})$ is a pair of a relation schema and relation content. A *database instance*, \underline{I} , of the database \underline{D} with schema \underline{S} , is a set of tables $\{\underline{t}_1, \dots, \underline{t}_n\}$ for each relation in \underline{S} . When it is clear from context, we refer to a database instance as simply a *database*.

We do not extend the notation of using underline for relational algebra operations. Instead, relational algebra operations are overloaded and are used as both plain relational and variational operations. It should be clear from context when an operation is variational or not. We also extend relational algebra such that projection of an empty list of attributes is a valid query that returns an empty set of tuples. We define the *empty* query ε as shorthand for projecting an empty list of attributes, that is, $\varepsilon = \pi_{\{\cdot\}}q$, where q is any relational query.

3.2 Encoding Variability

We encode variability in terms of *features*. The *feature space*, F, of a variational database is a closed set of boolean variables called features. A feature $f \in F$ can be enabled (i.e., f = true) or disabled (f = false). Features describe the variability in a given variational scenario. For example, in the context of schema evolution, features can be generated from version numbers (e.g., features V_1 to V_3 and T_1 to T_3 in the motivating example, Table 1); for SPLs, the features can be adopted from the SPL feature set (e.g., the *edu* feature in our motivating example, Table 1); and for data integration, the features may represent different data sources.

Features are used at variation points to indicate which variants a particular element belongs to. Thus, enabling or disabling each of the features in the feature set produces a particular database *variant* where all variation has been removed. A *configuration* is a *total* function that maps every feature in the feature set to a boolean value. We represent a configuration by the set of enabled features. For example, in our motivating scenario, the configuration $\{V_3, T_1, edu\}$ represents a database variant where only features V_3 , T_1 , and *edu* are enabled (and the rest are disabled). This database variant contains relation schemas in the yellow cells of Table 1. We refer to a variant by the configuration that produces it, e.g., variant $\{V_3, T_1, edu\}$ refers to the variant produced by applying that configuration.

When describing variation points in the database, we need to refer to subsets of the configuration space. We do this with propositional formulas of features. Thus, such a propositional formula defines a condition that holds for a subset of configurations and their corresponding variants. For example, the propositional formula $\neg edu$ represents all variants of our motivating example where the *edu* feature is disabled, i.e., variant schemas of the left schema column. We call a propositional formula of features a *feature expression* and define it formally in Figure 1. The evaluation function of feature expressions $\mathbb{E}[\![e]\!]_c : \mathbf{E} \to \mathbf{C} \to \mathbf{B}$ simply substitutes each feature f in the expression e with the boolean value given by configuration c and then simplifies the propositional formula to a boolean value. For example, $\mathbb{E}[\![f_1 \lor f_2]\!]_{\{f_i\}} = \text{true} \lor \text{false} = \text{true}$, while $\mathbb{E}[\![f_1 \lor f_2]\!]_{\{f_i\}}$

¹This simplification does not limit our formalization or our implementation. In fact, our implementation allows attributes to have different types.

Feature expression syntax:

$f \in \mathbf{F}$			Feature Name
$b \in \mathbf{B}$::=	true false	Boolean Value
$e \in \mathbf{E}$::=	$b \mid f \mid \neg e \mid e \land e \mid e \lor e$	Feature Exp.
$c \in \mathbf{C}$:	$F \rightarrow B$	Configuration

Relations over feature expressions:

 $e_1 \equiv e_2 \text{ iff } \forall c \in \mathbf{C} : \mathbb{E}\llbracket e_1 \rrbracket_c = \mathbb{E}\llbracket e_2 \rrbracket_c$ $sat(e) \text{ iff } \exists c \in \mathbf{C} : \mathbb{E}\llbracket e \rrbracket_c = \text{true}$ $unsat(e) \text{ iff } \forall c \in \mathbf{C} : \mathbb{E}\llbracket e \rrbracket_c = \text{false}$

Figure 1. Feature expression syntax and relations.

false \lor false = false. Additionally, in Figure 1, we define a binary *equivalence relation* (\equiv) on feature expressions corresponding to logical equivalence, and unary *sat* and *unsat* predicates that determine whether a feature expression is satisfiable or unsatisfiable, respectively.

To incorporate feature expressions into the database, we *annotate* database elements (including attributes, relations, and tuples) with feature expressions. An *annotated element* x^e consists of an element x and a feature expression e called its *presence condition*. The presence condition determines under which configurations the element is present in the database. For example, assuming $\mathbf{F} = \{f_1, f_2\}$, the annotated number $2^{f_1 \vee f_2}$ is present in variants $\{f_1\}, \{f_2\}, \text{ and } \{f_1, f_2\}$ but not in variant $\{\}$. The operation $pc(x^e) = e$ returns the presence condition of an annotated element.

No matter the context, features are often related in ways that constrain the set of possible configurations. For example, only one of the temporal features of V_1-V_3 can be true for a given variant. This relationship (dependency) is captured by a feature expression, called a *feature model* and denoted by m, which restricts the set of *valid configurations*. That is, a configuration c is only valid if $\mathbb{E}[\![m]\!]_c = \text{true}$. For example, the restriction that at a given time only one of temporal features V_1-V_3 can be enabled is represented by the feature model $V_1 \oplus V_2 \oplus V_3$, where $f_1 \oplus f_2 \oplus \ldots \oplus f_n$ is syntactic sugar for $(f_1 \wedge \neg f_2 \wedge \ldots \wedge \neg f_n) \lor (\neg f_1 \wedge f_2 \wedge \ldots \wedge \neg f_n) \lor (\neg f_1 \wedge \neg f_2 \wedge \ldots \wedge f_n)$, that is, the features are mutually exclusive.

3.3 Variational Sets

A variational set (v-set) $X = \{x_1^{e_1}, \ldots, x_n^{e_n}\}$ is a set of annotated elements [6, 21, 48]. We typically omit the presence condition true in a v-set, e.g., $4^{true} = 4$. Conceptually, a v-set represents many different plain sets simultaneously. Thus, a plain set \underline{X} is a variant of the v-set X corresponding to its configuration and it can be generated given the variant \underline{X} 's configuration c by evaluating the presence condition of each element with c and including the element if the said evaluation results in true and excluding

it otherwise. This is done by the *v*-set configuration function $\mathbb{X}[\![X]\!]_c$. For example, assume we have the feature space $\mathbf{F} = \{f_1, f_2\}$ and the v-set $X_1 = \{2^{f_1}, 3^{f_2}, 4\}$. X_1 represents four plain sets: $\{2, 3, 4\} = \mathbb{X}[\![X_1]\!]_{\{f_1, f_2\}}$, i.e., the variant $\{2, 3, 4\}$ is generated from the v-set X_1 under the configuration $f_1 = \text{true}, f_2 = \text{true}; \{2, 4\} = \mathbb{X}[\![X_1]\!]_{\{f_1\}}; \{3, 4\} = \mathbb{X}[\![X_1]\!]_{\{f_2\}};$ and $\{4\} = \mathbb{X}[\![X_1]\!]_{\{\}}$. Following database notational conventions we drop the brackets of a v-set when used in database schema definitions and queries.

A v-set itself can also be annotated with a feature expression. $X^e = \{x_1^{e_1}, \dots, x_n^{e_n}\}^e$ is an *annotated v-set* where the feature expression e additionally applies to all elements in the v-set. The *normalization* operation $\downarrow (X^e)$ applies this constraint by pushing it into the presence conditions of the individual elements: $\downarrow (X^e) = \{x_i^{e_i \wedge e} \mid x_i^{e_i} \in X^e, sat(e_i \wedge e)\}.$ Note that normalization also removes elements with unsatisfiable presence conditions and may be applied to an unannotated v-set X since $X^{true} = X$. For example, in the annotated v-set $X_1 = \{2^{f_1}, 3^{\neg f_2}, 4, 5^{f_3}\}^{f_1 \land f_2}$, all elements in the set only exist when both f_1 and f_2 are enabled. Thus, normalizing the v-set X_1 results in $\{2^{f_1 \wedge f_2}, 4^{f_1 \wedge f_2}, 5^{f_1 \wedge f_2 \wedge f_3}\}$. The element 3 is dropped since $\neg sat(pc(3, X_1))$, where $pc(3, X_1) =$ $\neg f_2 \land (f_1 \land f_2)$. We use the function $pc(x, X^e)$ to return the presence condition of a unique variational element within a bigger variational structure.

We define several operations over v-sets [5]; these operations are used in Section 5.2. The semantics of a v-set operation is equivalent to applying the corresponding plain set operation to every corresponding variant of the argument v-sets. For example, the union of two v-sets $X_1 \cup X_2$ should produce a new v-set X_3 such that $\forall c \in \mathbb{C}$. $\mathbb{X}[\![X_3]\!]_c = \mathbb{X}[\![X_1]\!]_c \cup \mathbb{X}[\![X_2]\!]_c$, where \cup is the plain set union operation.

4 Variational Databases

To incorporate variability within a database, we annotate elements with feature expressions, as introduced in Section 3.2. We use annotated elements both in the schema and content. Within a schema we allow attributes and relations to exist conditionally based on the feature expression assigned to them (Section 4.1). At the content level, we annotate each tuple with a feature expression, indicating when the tuple is present (Section 4.2).

4.1 Variational Schemas

A variational schema captures variation in the structure of a database by indicating which attributes and relations are included or excluded in which variants. To this end, we annotate attributes, relations, and the schema itself with feature expressions, which describe the conditions under which each is present. A *variational relation schema* (*v*-*relation schema*), *s*, is a relation name with an annotated v-set of attributes, $s \in \mathbf{R} := r (A)^e$, where *A* is a v-set of attributes. The presence condition of the v-relation schema, *e*, determines in what variants of the database the relation itself is present. A *variational schema* (*v*-*schema*) is an annotated set of v-relation schemas, $S \in S := \{s_1, \ldots, s_n\}^m$. The presence condition of the entire v-schema, *m*, is the VDB's feature model, which provides a top-level constraint on the set of valid configurations, as described in Section 3.2. Hence, the v-schema defines all valid schema variants of a VDB.

Example 4.1. S_1 is the v-schema of a VDB that only contains relation emploi in Table 1 and has the feature space $\mathbf{F} = \{V_1, V_2, V_3\}$. Note that attributes that exist conditionally are annotated with a feature expression to account for such a condition, e.g., the name attribute only exists when $V_2 = \text{true}$.

$$S_1 = \{empbio(empno, sex, birthdate, name^{V_2}, firstname^{V_3}, \\ lastname^{V_3})\}^{m_1}$$

where $m_1 = V_1 \oplus V_2 \oplus V_3$.

where m_1 allows only one temporal feature for the basic schema to be enabled at a time.

The presence of an attribute follows the hierarchal layout of information in a database: an attribute's presence depends on the presence of its parent v-relation, which in turn depends on the presence of the v-schema. Thus, the complete presence condition of the attribute a^{e_a} in vrelation $r(\ldots)^{e_r}$ defined in v-schema *S* with feature model *m* is $pc(a, S) = e_a \wedge e_r \wedge m$.

Similarly, the presence condition of v-relation *r* is $pc(r, S) = e_r \wedge m$. For example, in Example 4.1 we have $pc(empbio, S_1) = V_3 \wedge m_1$. Furthermore, a database element is only present in a variant for which evaluation of its presence condition under the variant's configuration is true, e.g., in Example 4.1 the *name* attribute is present in the variant $\{V_2\}$ because $\mathbb{E}[\![pc(name, S_1)]\!]_{\{V_2\}} = \mathbb{E}[\![V_3 \wedge \text{true} \wedge m_1]\!]_{\{V_2\}} = \text{true} \wedge \text{true} \wedge (\text{false} \oplus \text{true} \oplus \text{false}) = \text{true}$ but it is not present in the variant $\{V_3\}$ since $\mathbb{E}[\![pc(name, S_1)]\!]_{\{V_3\}} = \text{false} \wedge \text{true} \wedge (\text{false} \oplus \text{false}) = \text{false}$.

Intuitively and similar to v-sets, a v-schema is a systematic compact representation of a set of plain schemas called variants. A schema variant can be obtained by *configuring* the v-schema with that variant's configuration [5].

4.2 Variational Tables

Variation also exists in database content. To account for content variability, we tag tuples with presence conditions. Thus, a *variational tuple* (*v*-*tuple*) is an annotated tuple, $u \in U := (v_1, \ldots, v_l)^{e_u}$. A v-tuple corresponds to a v-relation, $r(a_1, \ldots, a_l)^{e_r}$, where each element v_i is a value corresponding to attribute a_i (recall that attributes in a v-relation are ordered). For example, $(38, PL, 678)^{T_3}$ is a v-tuple that belongs to the *ecourse* relation from Example 4.1 and is only present when T_3 is enabled. The content of a v-relation is a set of v-tuples, $U \in \mathbf{T} := \{u_1, \ldots, u_k\}$ and a *variational table* (*v*-*table*) is the pair of its relation schema and content,

t = (s, U). A variational database instance is a set of v-tables, $I \in I ::= \{t_1, \ldots, t_n\}^m$. A VDB instance is well-formed if its encoded variation at the schema and content level are consistent and satisfiable [8].

Similar to a v-schema, a user can configure a v-table or a VDB for a specific variant [5]. This allows users to deploy a VDB for a specific configuration and generate the corresponding VDB variant. Additionally, our VDB framework puts all variants of a database into one VDB and it keeps track of which variant a tuple belongs to by annotating them with presence conditions. For example, consider tuples $(38, PL, 678)^{T_3}$ and $(23, DB, NULL)^{T_2}$ that belong to the *ecourse* table. The presence conditions T_3 and T_2 state that these tuples belong to temporal variants four and five of this VDB, respectively.

Our VDB framework encodes variation in databases at two levels: schema and content. While content-level variation can stand on its own, such as frameworks used for database versioning and experimental databases [26], the schema level cannot, e.g., *ecourse* (*courseno, coursename, deptno*^{T₃})^{*edu*∧(T₂∨T₃)} encodes variation at the schema level for variants of relation *ecourse* in Table 1. Dropping the presence conditions of tuples leads to ambiguity, i.e., it is unclear which variant each of the tuples (38, *PL*, 678) and (23, *DB*, NULL) belongs to. We can only guess that they belong to variants where T_2 or T_3 are enabled, but, we do not know for sure which one.

Note that we limit the granularity of content variation to tuples, that is, individual values within a tuple are not variational. This design decision causes some redundancy. For example, the tuples $(38, PL, 678)^{T_3}$ and $(38, PL, NULL)^{-T_3}$ cannot be represented as a single tuple with variation in the third element. However, this design decision does not prevent us from distinguishing between a NULL value that represents a missing value and a NULL value that represents a cell that is not present. This distinction can be made by checking the satisfiability of the presence condition of the value v_i in tuple u of relation r in schema S: If $sat(pc(v_i, u))$ then the NULL indicates a missing value and otherwise it indicates a nonpresent cell, where $pc(v_i, u) = e_u \land pc(r, S) \land pc(att(i), r)$.

5 Variational Queries

The variational nature of a VDB requires a query language that accounts for variation directly. We formally define *variational relational algebra* (VRA) in Section 5.1 as our algebraic query language. A query written in VRA is called a *variational query* (*v-query*), though we often just say *query* when it is clear from context. Unlike relational queries that convey an intent over a single database, a v-query typically conveys the same intent over several relational database variants. However, a single v-query is also capable of capturing different intents over different database variants.

Due to the expressiveness of v-queries, we define a type system for VRA that statically checks a v-query against the

Operators:

q

Variational conditions:

Variational queries:

$\in \mathbf{Q}$::=	r	Relation
		$\sigma_{ heta} q$	Selection
		$\pi_A q$	Projection
		$e\langle q,q\rangle$	Choice
		$q \times q$	Cartesian Product
		$q \circ q$	Set Operation
		ε	Empty Relation

Figure 2. Syntax of variational relational algebra.

underlying v-schema in Section 5.2. To make v-queries more useable we relieve the user from repeating the v-schema's variation in their v-queries. This is achieved by explicitly annotating queries in Section 5.3. We then define the *variationpreservation* property for VRA at the type level in Section 5.4.

5.1 Variational Relational Algebra

To account for variation, VRA combines relational algebra (RA) with *choices* [20, 27, 47]. A choice $e\langle x_1, x_2 \rangle$ consists of a feature expression *e*, called the *dimension* of the choice, and two *alternatives* x_1 and x_2 . For a given configuration *c*, the choice $e\langle x_1, x_2 \rangle$ can be replaced by x_1 if *e* evaluates to true under configuration *c*, (i.e., $\mathbb{E}[\![e]\!]_c$), or x_2 otherwise.

Figure 2 defines the syntax of VRA. The selection operation is similar to standard RA selection except that the condition parameter is variational meaning that it may contain choices. For example, the query $\sigma_{e\langle a_1=a_2,a_1=a_3\rangle}r$ selects a vtuple *u* if it satisfies the condition $a_1 = a_2$ and $sat(e \land pc(u))$ or if $a_1 = a_3$ and $sat(\neg e \land pc(u))$. The projection operation is parameterized by a v-set of attributes, A. For example, the query $\pi_{a_1,a_2} r$ projects a_1 from relation r unconditionally, and a_2 when sat(e). The choice operation enables combining two v-queries to be used in different variants based on the dimension. In practice, it is often useful to return information in some variants and nothing in others. We introduce an explicit *empty* query ε to facilitate this. Similar to our definition of the empty query for relational algebra, for VRA we also have: $\varepsilon = \pi_{\{\}}q$. The empty query is used, for example, in q_2 in Example 5.1. The rest of VRA's operations are similar to RA, where all set operations (union, intersection, and product) are changed to the corresponding v-set operations.

Our implementation of VRA also provides mechanisms for renaming queries and qualifying attributes with relation/subquery names. These features are needed to support self joins and to project attributes with the same name in different relations. However, for simplicity, we omit these features from the formal definition in this paper.

The result of a v-query is a v-table with the reserved relation name *result*. For example, assume that v-tuples $(1, 2)^{f_1}$ and $(3, 4)^{\neg f_3}$ belong to a v-relation $r(a_1, a_2)$, which is the only relation in a VDB with the trivial feature model true. The query $f_3 \langle \pi_{a_1} f_2, r, \varepsilon \rangle$ returns a v-table with relation schema *result* $(a_1 f_2)^{f_3}$, which indicates that the result is only nonempty when f_3 is true and that the result includes attribute a_1 when f_2 is true. The content of the result relation for the example query is a single v-tuple $(1)^{f_1}$. The tuple $(3)^{\neg f_3}$ is not included since the projection occurs in the context of a choice in f_3 , which is incompatible with the presence condition of the tuple, i.e., $unsat(f_3 \land \neg f_3)$. This illustrates how choices can effectively filter the tuples in a VDB based on the dimension. Example 5.1 illustrates how a v-query can be used to express variational information needs.

Example 5.1. Assume we have the VDB introduced in Example 4.1. The user wants the employee ID numbers (empno) and names for variants $\{V_2\}$ and $\{V_3\}$. The user needs to project the name attribute for variant $\{V_2\}$, the firstname and lastname attributes for variant $\{V_3\}$, and empno attribute for both variants. This can be expressed with the following v-query.

$q_1 = \pi_{empno^{V_2 \vee V_3}, name, firstname, lastname} emploi$

In the example, note that the user does not need to repeat the variability encoded in the v-schema in their query, that is, they do not need to annotate name, firstname, and *lastname* with V_2 , V_3 , and V_3 , respectively. We discuss this in more detail in Section 5.3. q_1 queries all three variants simultaneously although the returned results are only associated with variants V_2 and V_3 due to the annotation of the attribute *empno* in the query and the presence conditions of the rest of the projected attributes in the schema. Yet, the query can be more simplified with a choice. q_2 selects only two out of the three variants explicitly: $q_2 =$ $V_2 \lor V_3 \langle \pi_{empno,name,firstname,lastname} empbio, \varepsilon \rangle$. Note that queries q_1 and q_2 return the same set of v-tuples since neither returns tuples associated with variant V_1 , but their returned v-tables have different presence conditions, thus, q_2 filters out tuples that belong to variant V_1 while q_1 does not.

Expressing the same intent over several database variants by a single query relieves the DBA from maintaining separate queries for different variants or configurations of the schema. Example 5.2 illustrates this point.

Example 5.2. Assume a VDB with $\mathbf{F} = \{V_1, V_2, V_3\}$ and the corresponding basic schema variants in Table 1. The user wants to get all employee names across all variants. They express this

$$\begin{split} \mathbb{Q}[\![.]: \mathbf{Q} \to \mathbf{C} \to \mathbf{Q} \\ \mathbb{Q}[\![r]\!]_c &= \mathbb{R}[\![r]\!]_c = \underline{r} \\ \mathbb{Q}[\![\sigma_{\theta}q]\!]_c &= \sigma_{\mathbb{C}[\![\theta]\!]_c} \mathbb{Q}[\![q]\!]_c \\ \mathbb{Q}[\![\pi_A q]\!]_c &= \pi_{\mathbb{A}[\![A]\!]_c} \mathbb{Q}[\![q]\!]_c \\ \mathbb{Q}[\![e\langle q_1, q_2 \rangle]\!]_c &= \begin{cases} \mathbb{Q}[\![q_1]\!]_c, \text{ if } \mathbb{E}[\![e]\!]_c = \text{true} \\ \mathbb{Q}[\![q_2]\!]_c, \text{ otherwise} \end{cases} \end{split}$$

Figure 3. Configuration of VRA. It assumes that the v-query is well-typed. $\mathbb{R}[\![.]\!]_c$, $\mathbb{C}[\![.]\!]_c$, and $\mathbb{A}[\![.]\!]_c$ are configuration of v-relation, v-condition, and v-set of attributes, respectively. This function is a trivial recursion for the rest of VRA operations and $\mathbb{Q}[\![\varepsilon]\!]_c = \varepsilon$.

intent by the query q_3 :

$$q_{3} = V_{1} \langle \pi_{name} empacct,$$

(V_{2} \times V_{3}) \langle \pi_{name, firstname, lastname} emptio, \varepsilon \rangle \rangle

Since the v-schema enforces that exactly one of $V_1 - V_3$ be enabled, we can simplify the query by omitting the final choice.

 $q_4 = V_1 \langle \pi_{name} empacct, \pi_{name, first name, last name} empbio \rangle$

In principle, v-queries can also express arbitrarily different intents over different database variants. However, we expect that v-queries are best used to capture single (or at least related) intents that vary in their realization since this is easier to understand and increases the potential for sharing in both the representation and execution of a v-query.

The *configuration* function maps a v-query under a configuration to a relational query, defined in Figure 3. Thus, a v-query can be understood as a set of relational queries that their results is gathered in a single table and tagged with the feature expression stating their variant. Users can deploy queries for a specific variant by configuring them. Example 5.3 illustrates configuring a query.

Example 5.3. Assume the underlying VDB has the v-schema $S_3 = \{r(a_1^{f_1}, a_2, a_3)^{f_1 \vee f_2}\}$ and $\mathbf{F} = \{f_1, f_2\}$. The v-query $q_5 = \pi_{a_1, a_2} f_1 \wedge f_2, a_3 f_2 r$ is configured to the following relational queries: $\mathbb{Q}[\![q_5]\!]_{\{f_1\}} = \mathbb{Q}[\![q_5]\!]_{\{\]} = \pi_{\underline{a}_1} \underline{r}, \mathbb{Q}[\![q_5]\!]_{\{f_2\}} = \pi_{\underline{a}_1, \underline{a}_3} \underline{r}, \mathbb{Q}[\![q_5]\!]_{\{f_1, f_2\}} = \pi_{\underline{a}_1, \underline{a}_2, \underline{a}_3} \underline{r}.$

VRA enables querying multiple database variants encoded as a singled VDB simultaneously and selectively. More precisely, VRA is *maximally expressive* in the sense that it can express any set of plain RA queries over any subset of relational database variants encoded as a VDB. We prove this claim in Theorem 5.4.

Theorem 5.4. Given a set of plain RA queries $\underline{q}_1, \ldots, \underline{q}_n$ where each query \underline{q}_i is to be executed over a disjoint subset I_i of variants of the VDB instance I, there exists a v-query qsuch that $\forall c \in \mathbb{C}$. $\mathbb{I}[I]_c = I_i \implies \mathbb{Q}[[q]]_c = \underline{q}_i$. *Proof.* By construction. Let f_i be the feature expression that uniquely characterizes the variants in each I_i . Then $q = (f_1 \land \neg f_2 \land \ldots \land \neg f_n) \langle \underline{q}_1, (f_2 \land \ldots \land \neg f_n) \langle \underline{q}_2, \ldots f_n \langle \underline{q}_n, \varepsilon \rangle \ldots \rangle$. \Box

The above construction relies on the fact that every RA query is a valid VRA (sub)query in which every presence condition is true. Of course, in most realistic scenarios, we expect that v-queries can be encoded more efficiently by sharing commonalities and embedding relevant choices and presence conditions within the v-query.

5.2 Well-Typed Queries

In this section, we introduce a static type system for VRA. The type system ensures that queries are consistent with the underlying variational schema. That is, that all referenced relations and attributes are present in the variation contexts in which they are used. For example, consider the VDB from Example 5.3 that contains only the relation $r(a_1^{f_1}, a_2, a_3)^{f_1 \lor f_2}$. The query $\pi_{a_4}r$ is ill-typed since a_4 is not present in r. Similarly, the queries $\pi_{a_1\neg f_1}r$ and $f_1\langle \pi_{a_2}r, \pi_{a_1}r \rangle$ are both ill-typed since a_1 is not present in r when f_1 is disabled.

The type of a VRA query is a v-relation schema $result(A)^e$. However, since the relation name is the same for all queries, we shorten this to A^e , that is, an annotated v-set of attributes. The annotation e corresponds to the presence condition of the returned table. The presence conditions of attributes within A may differ from the corresponding presence conditions in the original v-schema due to variation constraints imposed by the query. For example, continuing with relation $s = r(a_1f_1, a_2, a_3)f_1 \lor f_2$, the query $\pi_{a_2f_1}r$ has type $\{a_2f_1\}f_1 \lor f_2$. In the original schema, a_2 is present when $f_1 \lor f_2$, while in the query it is present only when f_1 is enabled.

Figure 4 defines a typing relation that relates VRA queries to their types. The judgment form $e, S \vdash q : A^{e'}$ states that in variation context e within v-schema S, v-query q has type $A^{e'}$. If a query does not have a type, it is *ill-typed*. A *variation context* is a feature expression that tracks which variants the current subquery is present in. We sometimes use the judgment form $S \vdash q : A^{e'}$ when the variation context is the unextended feature model, that is, $pc(S), S \vdash q : A^{e'}$. We assume that the v-set of attributes A is normalized to remove elements with unsatisfiable presence conditions, but this normalization is only shown explicitly in the rules where strictly necessary.

The rule RELATION-E looks up relation r in the v-schema S and returns its v-set of attributes A. The presence condition of A is the conjunction of the relation's presence condition in the v-schema, e', the current variation context, e, and the feature model, pc(S). In this way, the type is constrained to reflect both the constraints present in the v-schema and the context of the relation reference in the query. The last premise ensures that the relation exists in at least one variant by checking that the type's presence condition is satisfiable.

VRA typing rules:

V-condition typing rules: (As a reminder, b: boolean tag, <u>a</u>: plain attribute, k: constant value):

Boolean-C $e, A \vdash b$	$\begin{array}{l} \text{AttOptVal-C} \\ a^{e'} \in A \qquad sat(e' \wedge e) \end{array}$	ATTOPTATT-C $a_1^{e_1} \in A$ $a_2^{e_2} \in A$ $sat(e_1 \land e_2 \land e)$	$\frac{\text{NeG-C}}{e, A \vdash \theta}$
<i>e, A F v</i>	$e, A \vdash \underline{a} \bullet k$	$e, A \vdash \underline{a}_1 \bullet \underline{a}_2$	
Conjunction-C $e, A \vdash \theta_1$ $e, A \vdash \theta_2$	Disjunction-C $e, A \vdash \theta_1$ $e, A \vdash \theta_2$	CHOICE-C $e \wedge e', A \vdash \theta_1$ $e \wedge \neg e', A \vdash \theta_2$	
$e, A \vdash \theta_1 \land \theta_2$	$e, A \vdash \theta_1 \lor \theta_2$	$e, A \vdash e' \langle \theta_1, \theta_2 \rangle$	

Figure 4. The rules assume that the underlying VDB is well-formed. Remember that our theory assumes all attributes have the same type and all constants belong to attributes' domain.

This means that referencing a relation in a context where it is never present is a type error.

For a projection $\pi_A q$, the rule PROJECT-E checks that all projected attributes A are present in at least one variant of the variation context (second premise) and that these attributes are *subsumed* by type of the subquery q (third premise). The subsumption relation A < A' used in the third premise is defined as $\forall a^{e_1} \in \downarrow (A) . \exists e_2. a^{e_2} \in \downarrow (A'), sat(e_1 \land e_2)$, which ensures that all of the projected attributes are present in the type of the subquery q, and that the presence conditions of the v-set of projected attributes do not contradict the presence conditions in the type of q. The result type is the vset intersection of the projected attributes and the attributes of the subquery ensuring that the variation constraints of both are captured.

The rule SELECT-E checks if its subquery and v-condition are well-typed and if so it returns the subquery's type. The v-condition typing relation is defined in Figure 4 and has the judgment form $e, A \vdash \theta$, which states that the v-condition θ is well-formed in variation context e within attribute v-set A. The v-condition typing rules ensure that each attribute used in a v-condition is present in A and that the presence condition associated with that attribute does not contradict the current variation context.

For a choice of queries $e'\langle q_1, q_2 \rangle$, the rule Choice-E recursively infers the type of each alternative subquery in a variation context extended to reflect which branch of the choice the subquery is contained in, that is, e' for q_1 and $\neg e'$ for q_2 . The result type of a choice is the v-set union of the types of the subqueries annotated by the disjunction of their presence conditions, reflecting that either one alternative will be chosen or the other. Note that CHOICE-E is the only rule that refines the variation context.

The EMPTYRELATION-E rule states that an empty relation has the type of an empty set annotated by false, which is the required base case to ensure that the type system is variation preserving (see Section 5.4). The remaining rules are straightforward extensions of the standard relational algebra typing rules for product and set operations to account for variation contexts and v-sets.

5.3 Explicitly Annotating Queries

V-queries do not need to repeat information that can be inferred from the v-schema or the type of a query. For example, the query q_1 shown in Example 5.1 does not contradict the schema and thus is type correct. However, it does not include the presence conditions of attributes and the relation encoded in the schema while q_6 repeats this information.

$$q_6 = \pi_{empno^{V_2 \vee V_3}, name^{V_2}, firstname^{V_3}, lastname^{V_3}} (m_2 \langle empbio, \varepsilon \rangle)$$

,

Similarly, the projection in the query $q_7 = \pi_{name, firstname} subq_7$ where $subq_7 = V_2 \langle \pi_{name}q_6, \pi_{firstname}q_6 \rangle$ is written over S_1

$$\lfloor . \rfloor_{S} : \mathbf{Q} \to \mathbf{S} \to \mathbf{Q}$$

$$\lfloor r \rfloor_{S} = pc(r) \langle \pi_{A}r, \varepsilon \rangle \quad \text{where} \quad S \vdash r : A$$

$$\lfloor \pi_{A}q \rfloor_{S} = \pi_{A \cap A'} \lfloor q \rfloor_{S} \quad \text{where} \quad S \vdash \lfloor q \rfloor_{S} : A^{i}$$

$$\lfloor e \langle q_{1}, q_{2} \rangle \rfloor_{S} = e \langle \lfloor q_{1} \rfloor_{\downarrow(S^{e})}, \lfloor q_{2} \rfloor_{\downarrow(S^{\neg e})} \rangle$$

Figure 5. Explicitly annotating a well-typed query with a v-schema. This function is a trivial recursion for the rest of VRA operations and $\lfloor \varepsilon \rfloor_S = \varepsilon$.

and it does not repeat the presence conditions of attributes from its $subq_7$'s type. The query $q_8 = \pi_{name^{V_2}, firstname^{-V_2}} subq_7$ makes the annotations of projected attributes *explicit* w.r.t. both the v-schema S_1 and its subquery's type. Although relieving the user from explicitly repeating variation makes VRA easier to use, queries still have to state variation explicitly to avoid losing information when decoupled from the schema. We do this by defining the function $\lfloor q \rfloor_S : \mathbf{Q} \rightarrow$ $\mathbf{S} \rightarrow \mathbf{Q}$, that *explicitly annotates a query q with the schema S*. The explicitly annotating query function, formally defined in Figure 5, conjoins attributes' and relations' presence conditions with the corresponding annotations in the query and wraps subqueries in a choice when needed. Note that, q_8 and q_6 are $\lfloor q_7 \rfloor_{S_1}$ and $\lfloor q_1 \rfloor_{S_1}$, respectively, after simplification.

Theorem 5.5. *If the query q has the type A then its explicitly annotated counterpart has the same type A, i.e.:*

 $S \vdash q : A \Longrightarrow S \vdash \lfloor q \rfloor_S : A' \text{ and } A \equiv A'$

This shows that the type system applies the schema to the type of a query although it does not apply it to the query. The type equivalence is v-set equivalence for normalized v-set of attributes.

We have proved Theorem 5.5 in the Coq proof assistant [31].

5.4 Variation-Preservation Property

To show that VRA is type safe we benefit from RA's type safety [36] by defining the *variation-preservation* property for VRA which connects VRA to RA. The variation-preservation property states that if a query q has type A then configuring the type of a valid explicitly annotated query is the same as the type of its corresponding configured query. Theorem 5.6 proves this property.

Theorem 5.6 is visualized by the commuting diagram below, where the vertical arrows indicate corresponding configure functions, *type* indicates VRA's type system, i.e., $type(q) = A^e$ is

$$\begin{array}{cccc} e & [q]_S \xrightarrow{\longrightarrow} A^e \\ \hline e & \mathbb{Q}[.]_c & \stackrel{i}{\downarrow} & \stackrel{i}{\downarrow} \mathbb{A}[.]_c \\ \hline g & \stackrel{i}{\downarrow} & \stackrel{i}{\downarrow} \underbrace{type} \xrightarrow{A} \\ \hline g & \stackrel{i}{\longrightarrow} \underline{A} \end{array}$$

 $S \vdash q : A^e$, and <u>type</u> indicates RA's type system, i.e., $\underline{S} \vdash \underline{q} : \underline{A}$. We assume that the v-schema and schema are passed to the respective type systems. The diagram states that if we configure q with c, then determine the type of the plain query q using the standard RA type system (the lower left path), GPCE '21, October 17-18, 2021, Chicago, IL, USA

we get the same type <u>A</u> as if we had instead inferred a variational type A for q using the VRA type system, then configure A with c (the upper right path). The variation-preservation property ensures that the type of a variational query encodes the types of all the plain queries it encodes.² The query must be explicitly annotated since the configuration function for v-queries does not take the v-schema into account.

Theorem 5.6. For all configurations c, if a query q has type A then its configured query $\mathbb{Q}[\![\lfloor q \rfloor_S]\!]_c$ has type $\mathbb{A}[\![A]\!]_c$, i.e., $\forall c \in \mathbb{C}.S \vdash q : A \Rightarrow \mathbb{S}[\![S]\!]_c \vdash \mathbb{Q}[\![\lfloor q \rfloor_S]\!]_c : \mathbb{A}[\![A]\!]_c$

Proof. By structural induction. We proved this theorem in the Coq proof assistant [31]. \Box

6 VDBMS Implementation

We implement a prototype of the VDB and VRA frameworks as the Variational Database Management System (VDBMS). VDBMS is implemented in Haskell and sits on top of any standard relational DBMS. Data is stored in the form of vtables, explained in Section 4.2. The presence conditions on tuples are stored as an additional attribute in each table. All of the other presence conditions in our framework are stored either in the Haskell layer or in a separate metadata table in the underlying database. To support running VDBMS with multiple different plain relational DBMS backends, we provide a shared interface for communicating with the backend DBMS and instantiate it for different database engines such as PostgreSQL and MySQL. An expert can extend VDBMS to another database engine by writing methods for connecting to and querying the database.

6.1 VDBMS Architecture

Figure 6 shows the architecture of VDBMS. The VDB and its v-schema are stored in the DBMS, shown in the bottom right. A VDB can be *configured* to its plain relational database variants for deployment. For example, an SPL developer may configure a VDB to produce the plain relational database to accompany a software product for a client.

To extract information from a VDB, a user inputs a v-query q to VDBMS. First, q is checked by the *type system*. If the query is ill-typed, the user gets an error explaining what part of the query violated the v-schema. Otherwise, q is explicitly annotated with information from the schema and passed to the *variation minimization* module. This module simplifies the query based on syntactic rules [5] that preserve the semantics of the query. These rules make VRA flexible since an information need can be represented by multiple different v-queries as demonstrated in Example 5.1 and Example 5.2. The simplified query is then sent to the *generator* module where SQL queries are generated from v-queries by different approaches explained in Section 6.2. The generated SQL

²We have also defined this property at the semantics level to show that *running* a variational query corresponds to running all of its variants on all of the variants of the VDB [5].



Figure 6. VDBMS architecture. The dotted double-line from the input v-query indicates the dependency of passing the v-query to this module only if it is well-typed.

queries are then executed on the underlying DBMS yielding one or more v-tables. These are passed to the *v-table builder*, which combines them into a single v-table to be returned to the user. The v-table builder cleans up the resulting v-table by filtering out duplicate and invalid tuples, and shrinking presence conditions.

6.2 SQL Generators

Since VDBMS sits on top of a plain relational DBMS, vqueries must be translated into (sets of) plain relational queries. We have explored multiple different *SQL generators* for v-queries. In the descriptions below, we focus on the differences among each approach. However, each of these generators must also add relation qualifiers to attributes, rename subqueries where appropriate, and extend the list of projected attributes to include the special presence condition attribute stored with each v-table. The resulting v-tables produced by each approach are passed to the v-table builder to be combined into a single resulting v-table.

Given an explicitly annotated, well-typed v-query q, we explored five approaches to generate SQL queries for q:

1. *Naive Brute Force (NBF)*: Configures *q* into a set of RA queries corresponding to each valid configuration of *q*.

2. Unique Brute Force (UBF): Like NBF except that we only generate SQL queries for unique RA queries produced by configuring *q*.

3. *Union-All-Variants (UAV)*: Takes the SQL queries generated by UBF and unions them into a single SQL query. To do so, it forces all of the SQL queries to return the same relation schema. Additionally, it applies the presence condition of each SQL query to its tuples by concatenating it with the presence condition attribute in the projected attribute set.

4. *Injected Naive Brute Force (NBF(i))*: Similar to NBF, except that the feature expression associated with each configuration is injected into the SQL query. This simplifies the

job of the v-table builder, which must only fix the schema of the returned tables rather than modifying the presence conditions of all returned tuples.

5. *Injected Unique Brute Force (UBF(i))*: The same idea as NBF(i), except applied to the UBF approach.

The SQL generators produce queries in a generic query format that can be rendered into concrete SQL queries executable on each underlying DBMS engine. Each of these approaches conduct the same essential tasks. However, they vary in where they enforce variation preservation. For example, UAV, NBF(i), and UBF(i) generate queries that preserve variation by construction, while NBF and UBF yield intermediate v-tables that violate variation preservation and then recover this property in the v-table builder module. A complete description of each of the approaches, and examples of the SQL queries generated for each, can be found in [5].

7 Experiments and Discussion

In this section, we compare the performance of VDBMS with the different SQL generation approaches described in Section 6.2. Note that this is not intended as a comprehensive empirical evaluation. The main contributions of this work are the new functionality that VDBMS adds to traditional RDBMSs, the formal model of variational databases described in Section 4, and the theoretical results described in Section 5. These experiments are rather provided as a demonstration that our approach works as described and to facilitate discussion of implementation design decisions.

For our experiments, we use two previously developed datasets [8], both of which are available³ online:

1. An *email SPL* VDB, which illustrates database variation for an email system SPL. The feature model is taken from [23] with some simplifications, resulting in eight features with five database variants. The data is taken from the Enron corpus⁴ and is adapted based on the needs of the SPL. The v-queries were written to resolve the feature interactions in the email SPL described in [23].

2. An *employee evolution* VDB, which illustrates the application of VDBMS to schema evolution. The schema, its evolution, and queries are taken from [34] with some adaptation. It has five features denoting each time the schema evolved, which results in five database variants. The data is from a real-world employee database.⁵

We use these datasets to ensure the correctness of each approach and compare them. To ensure our SQL generator methods are implemented correctly we conducted two *sanity checks* for all v-queries that yield runnable SQL queries, which passed for every combination of approach and dataset:

1. We check that the variation-preservation property holds. That is, we check that for all configurations, configuring the

³https://zenodo.org/record/4321921

⁴http://www.ahschulz.de/enron-email-data/

⁵https://github.com/datacharmer/test_db



(b) The email VDB.

Figure 7. Comparison of SQL generators NBF, NBF(i), UAV, UBF, and UBF(i).

resulting v-table is the same as running an identically configured query over the corresponding configured database.

2. We check that the results from each pair of methods are equivalent.

We compare the runtime of each of our approaches to executing queries. The runtime contains all elements of executing a query, including type checking, annotation, optimization, SQL generation, and v-table building. We run the experiments on a MacBook Pro with a 2.4 GHz Core i7 processor and 8 GB of 1600 MHz DDR3 RAM. All experiments are run with PostgreSQL 13.3 as the database engine.

Figure 7 shows the runtime for each query for each of the introduced approaches in Section 6.2 over the employee and email VDBs. The queries are labeled at the top of the plots and the approaches are indicated by different color bars.

Figure 7a shows that NBF(i) is usually faster than NBF, but UBF and UBF(i) do not follow a similar pattern. Additionally, NBF(i), UAV, and UBF are close in performance and none consistently performs better than the others.

Figure 7b also shows that NBF(i) is consistently faster than NBF, and UBF(i) is also mostly faster than UBF for this dataset. While UAV mostly performs better than NBF(i), it is comparable to UBF(i) for this dataset. Yet, UAV sometimes generates a non-runnable SQL query due to forcing an attribute to have type string when it is projected as NULL [5]. This issue can be addressed by forcing the first subquery of the union to have all attributes projected and limiting the number of returned tuples to zero. This would force the type of attributes as they are in the schema and since it does not return any tuples it will not change the result.

Based on our experiments, the query construction (from type system to generating SQL queries) takes similar time between the approaches. Their main difference comes down to the gross runtime of queries on the VDB and building the v-table. UAV does not take any time to build a v-table since the result already has the desired schema and presence conditions, however, it spends more time on running the SQL query since queries generated by UAV are usually more complicated. On the other hand, although NBF and UBF run multiple SQL queries per v-query their generated SQL queries are simpler than the ones generated by UAV. However, in contrast to UAV, they must adjust the returned table for each SQL query and apply the correct presence condition to the tuples. Finally, the main difference between the performance of NBF and NBF(i) (and similarly, UBF and UBF(i)) is where they apply the correct presence condition to the tuples. While NBF(i) and UBF(i) pass this task to the underlying database engine (which seems to perform better) the NBF and UBF approaches do this task in the v-table builder, in the Haskell layer. Note that all four of these approaches still have to unify the schema of the returned tables to the v-table schema of the v-query.

8 Related Work

While variational databases provide a *generic* solution to the problem of variation in databases, lots of databases research has addressed *specific kinds* of variation. As described in Section 1, these more focused approaches often provide better solutions to one kind of variation but are less flexible and so not suitable for many applications. In the rest of this section, we briefly describe this databases research, and also describe previous work from the SPL community.

Schema evolution: Current solutions addressing schema evolution rely on temporal nature of it. They use timestamps as a means to track historical changes either in an external document [34] or as versions attached to databases [4, 13, 32, 42]. Some require the DBA to design a unified schema to support querying different versions [25], while others support migrating database variants to alternate versions [4, 13, 32, 42]. A third approach is to transform queries written against one version to other versions [34]. Temporal evolution is tracked by requiring the database to always have a time-related attribute in tables. Thus, queries have to specify the time frame for which they are inquiring information [34]. Now the user can choose a wide enough time frame in their queries to access to their desired variant(s). Unlike VDBs, schema evolution does not support expressing a variation need against two different variants at once, nor does it support expressing multiple information needs in a single query. **Data integration:** Data integration systems need to query disparate data sources which often have different formats and have been developed independently of each other [19]. Thus, work on *data integration* can be viewed as managing database variation in space at the content, schema, and format level. The ability to combine data in different formats (e.g., relational and unstructured data) is not supported by variational databases. In data integrated data and each data source has a wrapper/extractor that adjusts the schema and data of the source to the mediated schema [10, 18, 38]. Users query against the mediated schema, and the system assembles the results from the various sources. The set of wrapper/extractors collectively describe the variation among integrated systems, filling a role similar to our v-schemas.

A concern in data integration is tracking *data provenance*, that is, which sources the results of a query came from. Data provenance can be realized in variational databases by attaching a different feature to the tuples in each source. The variation preservation property ensures these features will be propagated to the query results.

Temporal databases and database versioning: Temporal databases [29, 37, 45] address scenarios where the state of the data at a specific time is important, such as financial and medical data. Some temporal databases extend traditional relational databases [2, 39, 46], while others adopt an in-database approach [30]. Temporal databases contain timestamps as one kind of value and queries may express conditions over timestamps [17, 28, 33]. Temporal databases only support content-level variation and are less expressive than VDBs in terms of the variation that they can describe. However, their special support for temporal values and conditions make expressing temporal constraints easier than an equivalent encoding in VDB/VRA, where one would have to introduce features for each timestamp and then use potentially large feature expressions to describe temporal ranges.

Database versioning aims to support collaborative data curation and analysis [11] by supporting non-linear, temporal changes to a database. Once such example is *OrpheusDB* [26], which is inspired by version control systems like Git. It captures different evolutions of the database in a version graph. A version graph can be viewed as a kind of variational database, although only one particular variant can be checked out at a time. ORPHEUSDB supports both git-style version control commands and SQL-like queries. Its query language *VQL* can query the data as well as their versions. VQL supports a subset of the query language for versioning and provenance proposed by Chavan et al. [15]. Similar to temporal databases, database versioning systems only support content-level variation.

Database variability in software development: A database may contain variation due to evolution of the business requirements of its associated software [24, 43]. Besides schema evolution and database migration other workarounds

have been proposed. The first is that a different relational database may be *specified and created per-variant*, according to the information needs of each variant [35]. This is labor-intensive and difficult to maintain since changes need to be propagated across variants manually. The second strategy is to define a single *global schema that applies to all variants* [9]. This strategy is more efficient to maintain, but can be complex and error prone in som some scenarios, such as SPL evolution [40, 41]. The third strategy is to define a *variable data model* [1, 40, 41] which models a database schema with annotations of features from the SPL to indicate their variable existence.

9 Conclusion and Future Work

We presented the variational database framework as a generic solution to encode and query multiple variants of a database as a single entity. The VDB framework systematically ensures that the variation in data and queries are encoded correctly and consistently, removing the burden of manual workarounds from database administrators and developers.

The VDB framework assumes a closed-world variation and configuration space, that is, the sets of features and configurations are closed. An immediate improvement would be to make the configuration and feature-space dynamically extensible. This is an essential piece to updating VDBs, which we do not yet address, since it would enable incrementally adding new variants to a VDB. Additionally, the performance of VDBMS can be improved by different optimizations, such as defining a user-defined type and functions for presence conditions in databases.

More speculatively, VDBMS could be made more usable by providing a visual interface that shows a snapshot of the database as the user writes their query. This improvement requires a type system that allows for holes in queries. This can be enriched by designing an error-tolerant type system that pinpoints where the user made a mistake in their query and allows the part of query that is well-typed to run [16].

Finally, although we have not implemented a system to generate a VDB for a variation scenario, it is trivial to do so if we have the variant databases. The problem is that, in most cases, the variant databases do not exist since current variation scenarios only simulate the effect of variation and do not incorporate it directly into the database or queries. Thus, an expert needs to manually generate the database variants. Another way to do this would be to extend the query language to support database updates, which would also significantly increase the applicability of our system.

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